

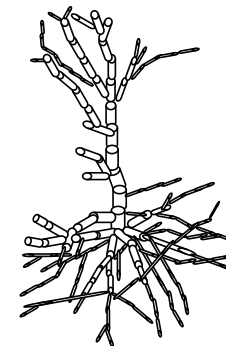
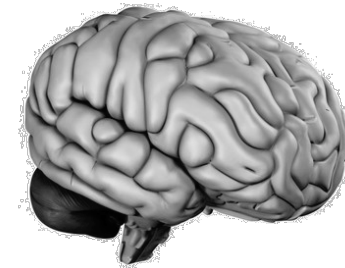
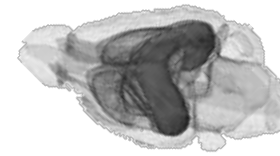


Simulation Codes in the Human Brain Project

Prof. Dr. Felix Schürmann
EPFL, CH

Some Numbers on the Brain

- Rat brain*
 - ~200M (2×10^8) nerve cells
 - ~130M glial cells
 - ~ $O(10^{12})$ synapses
- Human brain**
 - ~90B (10^{11}) nerve cells
 - ~90B glial cells
 - ~ $O(10^{15})$ synapses
- Each cell – a universe***
 - ~ $O(10B)$ proteins/nerve cell



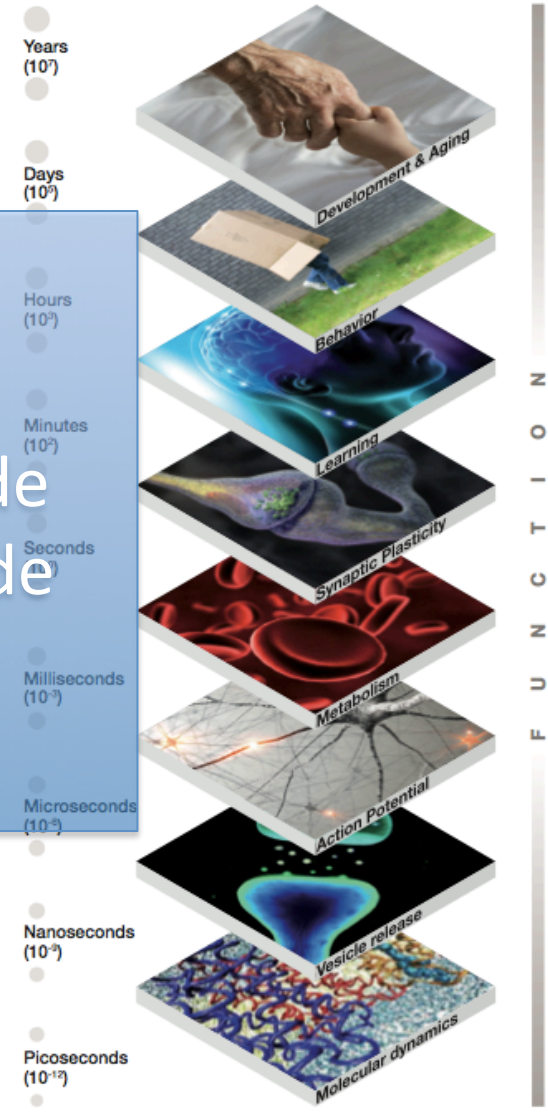
* Herculano-Houzel et al. 2006; **Herculano-Houzel 2009; *** Sims et al. 2007

Relevant Scales

Spatial Scales



Time scales



weak scaling

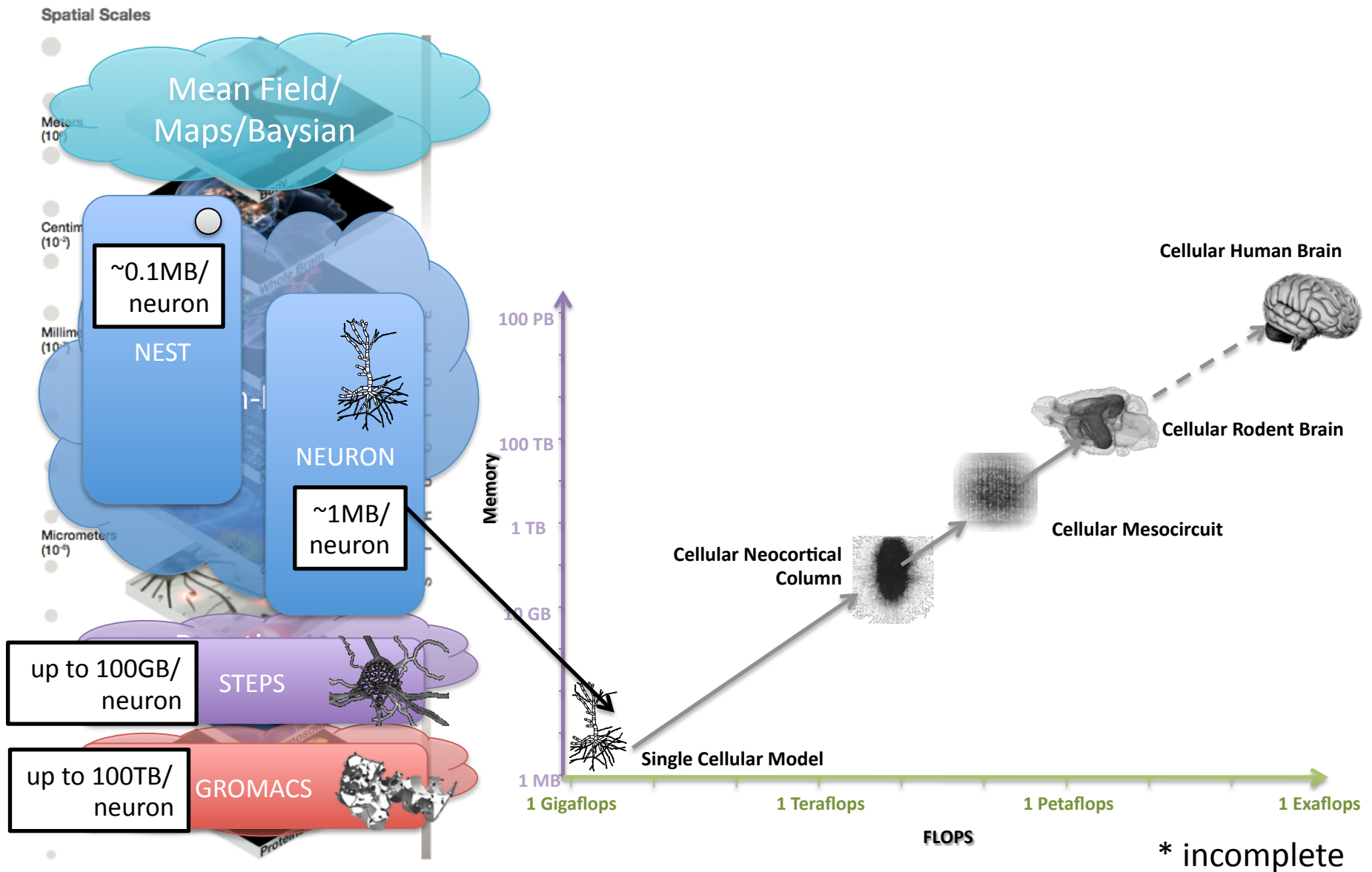
strong scaling

Space: ~ 9 orders of magnitude
Time: ~ 18 orders of magnitude

S
T
R
U
C
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U
R
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C
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I
O
N

Qualitative Simulator Landscape*



* incomplete

Simulation Codes in the HBP Ramp-up Phase



nest::
simulated()

<http://www.nest-initiative.org/>

Markus Diesmann, Hans-Ekkehard Plesser, Marc-Oliver Gewaltig
ODEs; loose (global) coupling

<http://www.neuron.yale.edu>

Michael Hines

ODEs, LinAlg; loose(global)/tight(specific) coupling



NEURON

for empirically-based simulations of neurons and networks of neurons

STEPS

STochastic Engine for Pathway Simulation



<http://www.nest-initiative.org/>

Erik De Schutter

Gillespie SSA, diffusion via NN coupling

- All are open source
- All have a scripting interface (python) for model setup
- All have C/C++ compute core
- All have their community mission and roadmap and HBP complements

In HBP: Anchored to the Neuron

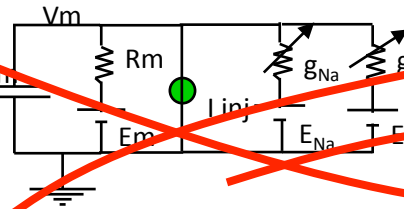
Point neuron, e.g. Izhikevich

$$v' = 0.04v^2 + 5v + 140 - u + I$$

$$u' = a(bv - u)$$

if $v = 30$ mV,
then $v \leftarrow c, u \leftarrow u + d$

Single Compartment HH model



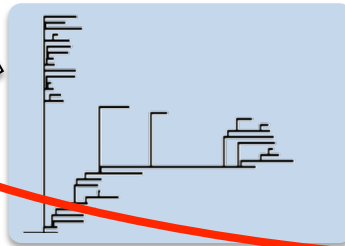
$$C_m \frac{dV_m}{dt} = \frac{E_m - V_m}{R_m} + I_{channels}$$

$$\frac{dm}{dt} = \alpha_m(V_m)(1 - m) - \beta_m(V_m)m$$

$$\frac{dh}{dt} = \alpha_h(V_m)(1 - h) - \beta_h(V_m)h$$

$$I_{channel} = m^n h g_{channel}(V_m - E_{channel})$$

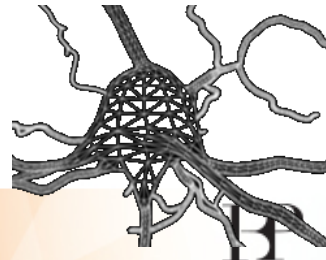
Multi Compartment HH model



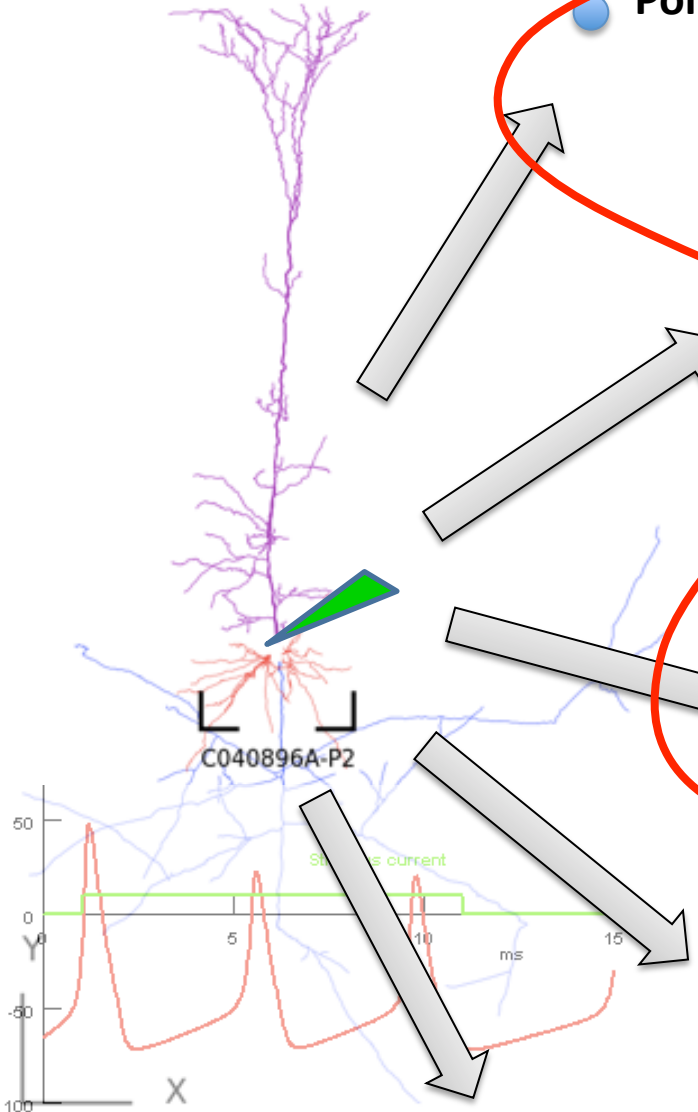
$$C_m \frac{dV_m}{dt} = \frac{E_m - V_m}{R_m} + I_{channels}$$

$$+ \frac{2(V_{m_{i+1}} - V_{m_i})}{R_{a_{i+1}} + R_a} + \frac{2(V_{m_{i-1}} - V_{m_i})}{R_{a_{i-1}} + R_a}$$

Reaction-Diffusion model

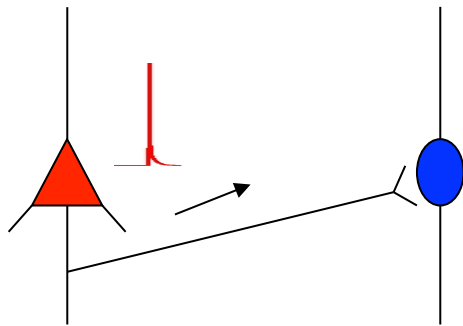


$$\dot{p}(\mathbf{x}; t) = -p(\mathbf{x}; t) \sum_{\mu=1}^M a_{\mu}(\mathbf{x}) + \sum_{\mu=1}^M p(\mathbf{x} - \mathbf{s}_{\mu}; t) a_{\mu}(\mathbf{x} - \mathbf{s}_{\mu})$$



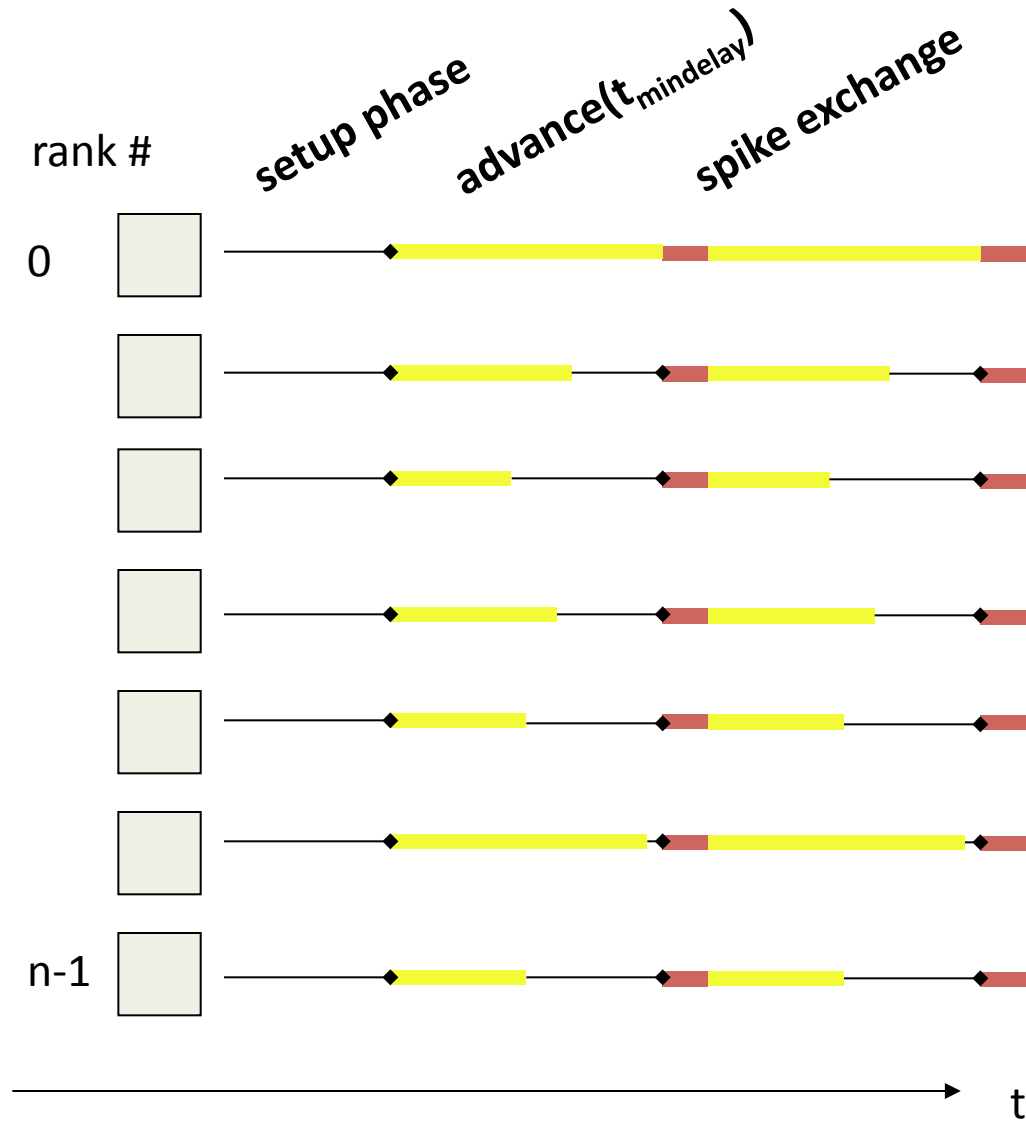
Coarse-Graining/MD

Useful Properties of Neuron-based Abstraction



$t_{\text{axonaldelay}}$

No spike evoked at time t can arrive at any postsynaptic cell sooner than $t + \min\{t_{\text{axonaldelay}}\}$



Initial Development Goals for NEST, NEURON

- Interactive Supercomputing
 - Use of dense memory; high memory bandwidth
 - Malleability (dynamical runtime)
 - Interaction with analysis and visualization frameworks
- Scalability (Communication, Memory!)
 - To support full brain scale models
 - Reduce memory footprint
- Software Engineering
 - Test driven development; Agile teams
 - Software lifecycle model
 - NEST has good practice
 - NEURON has a lot of legacy → coreNEURON
- Efficiency
 - Mini-Apps
 - Accelerator support while maintaining flexibility
 - Abstraction of SIMD

Subcellular Details

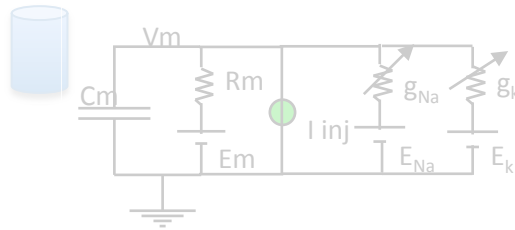
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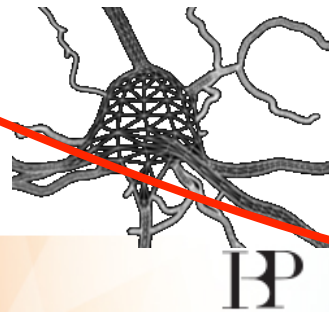
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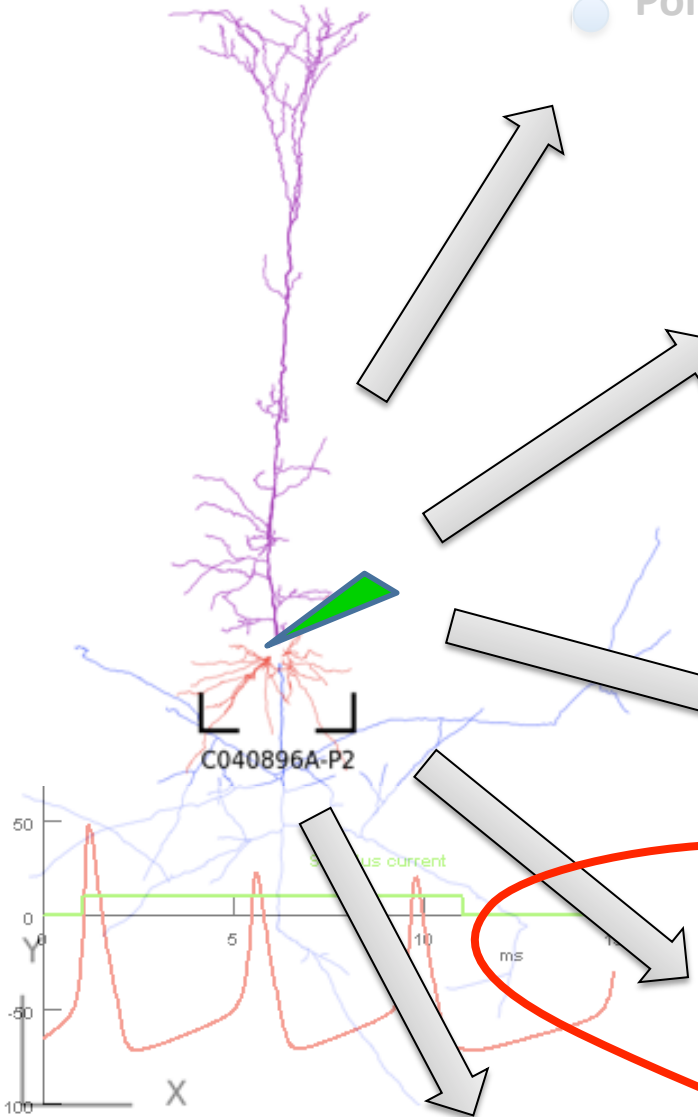
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$$\sum_{\mu=1}^M p(\mathbf{x} - \mathbf{s}_{\mu}; t) a_{\mu}(\mathbf{x} - \mathbf{s}_{\mu})$$

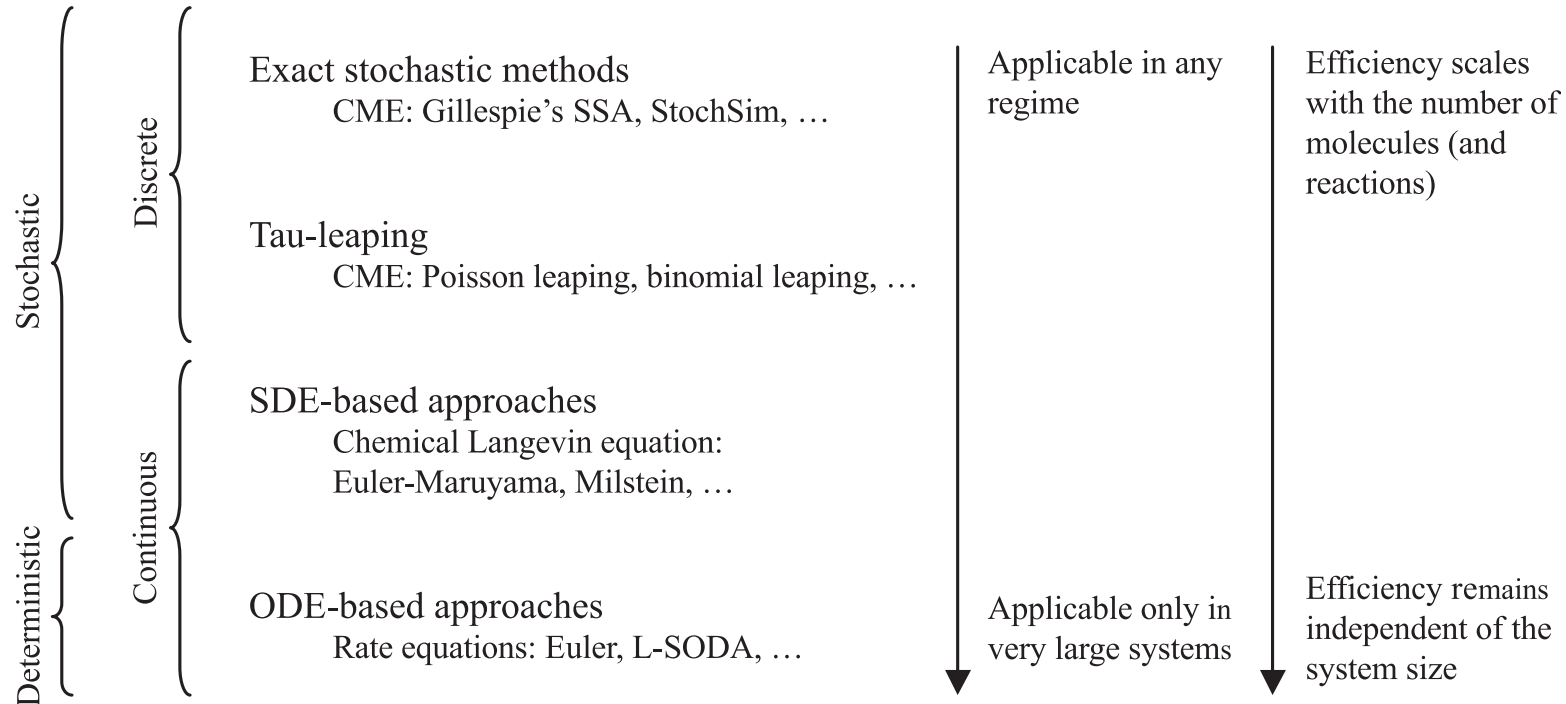


Coarse-Graining/MD

HP

Reaction... and...Diffusion

Reactions



Brownian Motion & Stochastic Diffusion

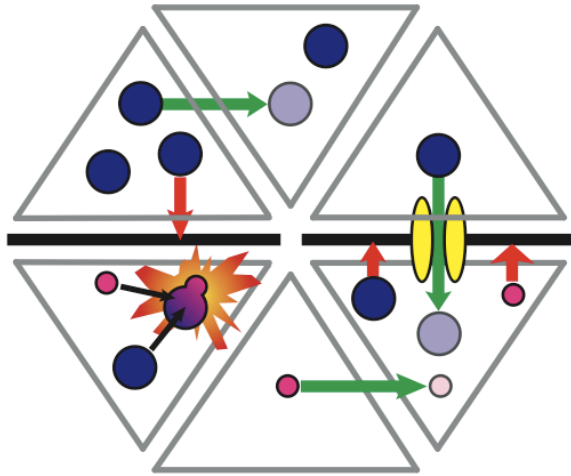
- General Finite Volume, Finite Element for PDEs
- Continuous Random Walk (e.g. MCell)
- Random Walk on discrete lattice
- Voxel-based methods (e.g. MesoRD, STEPS)

From:
 Computational Modeling Methods for Neuroscientists
 ed. Erik de Schutter

STEPS Simulator

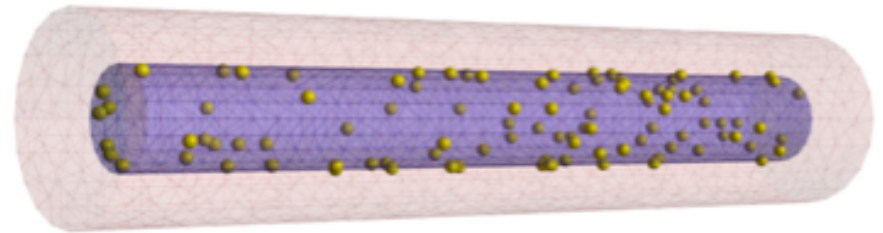
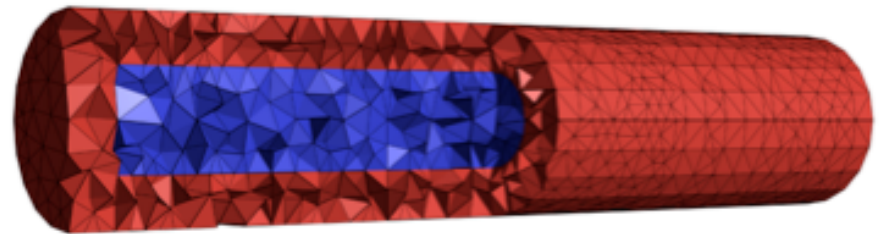
STochastic Engine for Pathway Simulation:

Simulation algorithm



- Each tetrahedron (grey) is a well-mixed volume, in which reactions can occur (Gillespie, 1977).
- Neighbouring tetrahedrons are coupled by diffusive fluxes.
- Triangles (black) act as boundaries and can also embed molecules. These can bind to ligands and transport volume molecules in between tetrahedrons belonging to different compartments.

$$\begin{aligned} \frac{d}{dt} Na_x^+ &= J_{leak,Na}^x - 3 J_{pump}^x + J_{stim}^x(t) \\ \frac{d}{dt} GLC_n &= J_{GLC}^{en} - J_{HKPFK}^n \\ \frac{d}{dt} GLC_g &= J_{GLC}^{cg} + J_{GLC}^{eg} - J_{HKPFK}^g \\ \frac{d}{dt} GAP_x &= 2 J_{HKPFK}^x - J_{PGK}^x \\ \frac{d}{dt} PEP_x &= J_{PGK}^x - J_{PK}^x \\ \frac{d}{dt} PYR_x &= J_{PK}^x - J_{LDH}^x - J_{mito,in}^x \\ \frac{d}{dt} LAC_n &= J_{LDH}^n - J_{LAC}^{ne} \end{aligned}$$



<http://steps.sourceforge.net/>

Erik De Schutter

Contacts

The Human Brain Project Consortium

<http://www.humanbrainproject.eu>

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Human Brain Project

